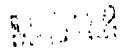
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BEAM HALO FORMATION FROM SPACE-CHARGE DOMINATED BEAMS IN UNIFORM FOCUSING CHANNELS

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Abstract

In space-charge dominated beams the nonlinear spacecharge forces produce a filamentation pattern, which results in a 2-component beam consisting of an inner core and an outer halo. The halo is very prominent in mismatched beams 1-3, and the potential for accelerator activation is of concern for a next generation of cw, highpower proton linaes that could be applied for intense neutron generators to process nuclear materials⁴. We present new results about beam halo and the evolution of space-charge dominated beams from multiparticle simulation of initial laminar beams in a uniform linear focusing channel, and from a model consisting of single particle interactions with a uniform-density beam core. We study the energy gain from particle interactions with the space-charge field of the core⁵, and we identify the resonant characteristic of this interaction as the basic cause of the separation of the beam into the two components⁶. We identify three different particles trajectory types, and we suggest that one of these types may lead to continuous halo growth, even after the halo is removed by collimators.

I. PHASE SPACE DYNAMICS FROM MULTIPARTICLE SIMULATION

We use multiparticle simulation to study the idealized problem of a round continuous beam in a uniform linear focusing channel with purely radial focusing. For the studies described in this paper, the computer code has been run with 3000 simulation particles through 56 steps per plasma period. We have chosen to study the dynamics of initial. Gaussian, laminar (zero-emittance) beams, where the initial density distributions are truncated at three standard deviations. In Fig. 1a we show the radial or r = r' phase space at 20 plasma periods for an initial mismatch. parameter M = 1.5, where the mismatch parameter gives the ratio of the initial beam radius to the matched radius We assign an initial positive radius to all particles, but if during the simulation a particle crosses the axis, we change the sign of the radius before plotting a point in r r' space. Fig. 1a shows the inner core and the outer halo. Idament as distinct structures. At present there is no established criterion for defining the halo. We define the core and the halo by choosing a core ethipse in it it space with the same Courant Snyder ellipse parameters as the rms ellipse with an emittance that we think encloses most of the core and excludes most of the halo

Fig. 1b shows the distribution at 20 plasma periods of particle energy $U_{\rm F}$ (the core appears, as the concentration of particles at small $U_{\rm F}$)

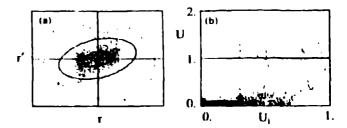


Figure 1. Results at 20 plasma periods from multiparticle simulation of an initial Gaussian-density laminar in a uniform linear focusing channel. The initial beam rms size in x is larger than the matched value by a factor M=1.5. We show a) r-r' phase space, b) particle energy U versus the initial particle energy U_1 .

All particle energies are normalized so that the particle with the maximum initial energy (largest initial radius) has $U_i = 1$. Fig. 1b shows that after 20 plasma periods, the beam does contain particles with U>1, which have more energy than the most energetic initial particle. The halo is mostly populated by the particles that have large initial energy, i.e., have large initial radius. However, a small fraction of particles with small initial radius (only one such particle is present in the 3000 particle run and it is not visible in the plot) also populate the halo, and the fraction of these halo particles with small initial energy increases rapidly with increasing mismatch parameter.

The characteristics of the beams after 20 plasma periods are shown in Table 1. All particle energies in Table 1 are normalized in the same way, to unity for the initial matched beam case. Column 1 shows the initial mismatch parameter M. Column 2 shows the values of the core emittance to rms emittance ratio. Column 5 shows that the maximum particle energy increases from the initial value by 10% for the matched case, and increases by 50% for a mismatch of M = 2.5. The last two columns show the percentage of final particles in the halo and the percentage of final particles with energy that exceeded the maximum initial particle energy. We see again that the percent of particles in the halo increases rapidly with increasing mismatch, and reaches a value of over 30% for an initial mismatch parameter of 2.5.

II. PHASE SPACE DYNAMICS FROM UNIFORM DENSITY CORE MODEL.

A. Energy Transfer Between a Single Particle and an Oscillating Core.

To gain some physical insight into what we observe in the simulation, we consider the model of a zero emittance, uniform density beam core of radius R, propagating in a uniform linear focusing channel. The transverse equation of motion of the beam radius is given by the envelope equation

$$\frac{d^2R}{dt^2} + \omega_0^2 R + \frac{K}{R} = 0,$$

where ω_0 is the natural frequency at zero current of a single particle, and nonrelativistically $K=q1/2\pi\epsilon_0 mv$, where q, m, and v are the charge, mass, and axial velocity of the particles, 1 is the beam current, and ϵ_0 is the permeability of tree space. For the matched beam $d^2R/dt^2=0$ and the matched beam radius is $R=R_0-\sqrt{K}/\omega_0$. The transverse equation of motion of a single test particle is

$$\frac{d^2x}{dt^2} + \omega_0^2 x - F_{SC} = 0,$$

where $F_{\mathcal{SC}}$ is the space charge force, given for a uniform density by

$$F_{SC} = \left\{ \begin{array}{ll} Kx / R^2 & x < R, \\ K / x, & x > R. \end{array} \right.$$

The particle energy is not constant because of the spacecharge repulsion of the core. For a matched core radius, there is no net change in energy averaged over a complete period of particle motion. For an oscillating, mismatched core there will in general be a net change in particle energy. For a small, radially symmetric core mismatch θR about the equilibrium radius R_0 , we can write for $x < R_1$

$$-\frac{d^2x}{dt^2} + A\Omega^2x\cos\Omega t = 0\,,$$

where $\delta R/R0$ A cos Ω 1 and Ω $\sqrt{2}\omega_0$. This approximate result is a special case of the Mathieu equation, and we expect periodic solutions in x for particle frequencies below half the core frequency Ω . When the particle frequency is half the core oscillation frequency, we expect a resonant growth of the x amplitude. The resonant condition requires a constant phase relationshap

between the particle and the core. We expect that the effect of the nonlinearity outside the core is to create a self limit to the resonance because of the change of frequency with amplitude, which causes a loss of phase coherence. The core oscillation causes a rate of energy gain for a particle within the beam core with velocity \hat{x} , given by

$$\frac{dU}{dt} : \vec{F} \bullet \hat{\vec{x}} = -A\Omega^2 \times \hat{x} \cos \Omega t$$

A particle that passes through the beam core can either gain energy, loose energy, or have no net energy change, depending on the relative phases of the particle displacement, the transverse velocity, and the core radius oscillation.

B. Trajectory Classification

A study of the trajectories of individual particles has been helpful for understanding the dynamics of the halo formation. The uniform core model described above provides an important reference point for such a study. We have numerically integrated the trajectories of particles through the field of the uniform core for the M = 1.5 case. launching particles with different initial x values, and with R = 1.5, R = 0, and $\dot{x} = 0$. We find three distinct classes of trajectories, which for the M = 1.5 case, we describe in terms of the initial x displacement as follows: a) For x < 1.5 the particles oscillate in phase with the core radius about their own equilibrium radius. These are stable radial plasma oscillations within the core, and we refer to these orbits as plasma trajectories, b) For x > 2.0the particles oscillate about the origin with an orbit in phase space that looks like an ellipse that is pinched inward along the velocity axis (the pinching is caused by the space charge force of the core). The amplitudes are variable and each orbit is confined to a narrow band in phase space. These particles occupy the halo and we call these orbits betatron trajectories, c) Finally, for 1.5 < x <2.0 the particles execute a more complex motion. They may initially spend part of the time executing plasma like oscillations within the core, after which they move into the proper phase relationship with respect to the core oscillations such that they can gain energy and move into an outer betatron like orbit in the halo. These particles can also reverse the pattern and return from the outer

Table 1
Beam Halo Characteristics at 20 Plasma Periods for Beams with Different Initial Mismatch

M	ecore/erms	U _{t,max}	Umax	$u_{\max}/u_{i,\max}$	% m halo	9 [1 .]
1,0	1	1 00	1.10	1.10	5,9	0.1
1.5	1	2.25	297	1.32	5.4	2.3
2.0	Ţ	4 00	5.90	1.48	16.	1 /
2,5	,1	6.25	9.38	1.50	31	2.0

betatron like orbit in the halo to a plasma like orbit within the core. We refer to these as hybrid trajectories, and we find that it is these particles that are most strongly affected by resonant energy transfer with the oscillating core, which can cause either energy loss into the core, or energy gain into the halo. Figure 2 shows examples of these trajectories in phase space traced >> 20 core oscillation periods using the uniform core is odel, with

eq. 1, and K = 1, launched with the following initial conditions R = 1.5, R = 0, and x = 0, and a) x = 1.0, b) x = 1.55, c) x = 1.65, and d) x = 2.2. The outlines of the core radius oscillation are shown on each of the plots, extending from x = (0.5743) to x = (1.50). These examples show a pure plasma trajectory in Fig. 2a, a hybrid trajectory that has not yet left the core in Fig. 2b,

a hybrid trajectory in the halo in Fig. 2c, and a periodic betairon trajectory in the halo in Fig. 2d.

The discovery of the hybrid trajectories is important because of the implications for the effectiveness of collimation. Suppose at a given time the beam is collimated to remove the existing halo. Any such collimation procedure, even if carried out under the most ideal of circumstances, would be able to remove only the particles with betatron trajectories and the particles with hybrid trajectories, which at that time populate the halo. Any hybrid orbits that are within the core at the time of collimation may be expected to gain energy at some later time and repopulate the halo. Therefore, while collimation does some good, its effectiveness would be limited by the percentage of hybrid particles that would repopulate the core within the time scale of interest. Although this may appear to be a serious limitation of the collimation, it appears in the uniform beam model that the 1.5 mismatch case is approximately x = 2.7. For this example collimation at a radius of 1.5 units could still be effective in limiting the amplitudes to less than $x = \pm 2.7$.

VI. ACKNOWLEDGMENTS

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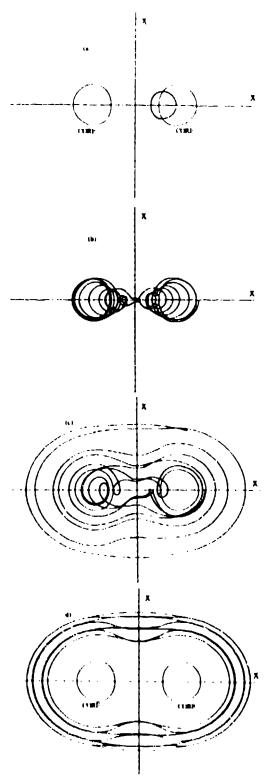


Fig. 2. Trajectories in phase space traced for 20 core oscillation periods using the uniform core model, with $m_{\rm O}=1$, and K=1, launched with the following initial conditions R=15, R=0, and x=0 and a) x=1,0, b) x=1,55, c) s=1,65, and d) x=2,2. The outlines of the core rad as oscillation are shown on each of the plots, extending from x=1,50 to x=-0,5,74,3 and from x=0,5,74,3 to x=1,50.